Abstract. The goal of this paper was to develop methods and protocols for water productivity mapping (WPM) using remote sensing data at multiple resolutions and scales in conjunction with field-plot data. The methods and protocols involved three broad categories: (a) Crop Productivity Mapping (CPM) (kg/m²); (b) Water Use (evapotranspiration) Mapping (WUM) (m³/m²); and (c) Water Productivity Mapping (WPM) (kg/m³). First, the CPMs were determined using remote sensing by: (i) Mapping crop types; (ii) modeling crop yield; and (iii) extrapolating models to larger areas. Second, WUM were derived using the Simplified Surface Energy Balance (SSEB) model. Finally, WPMs were produced by dividing CPMs and WUMs. The paper used data from Quickbird 2.44m, Indian Remote Sensing (IRS) Resourcesat-1 23.5m, Landsat-7 30m, and Moderate Resolution Imaging Spectroradiometer (MODIS) 250m and 500m, to demonstrate the methods for mapping water productivity (WP). In terms of physical water productivity (kilogram of yield produced per unit of water delivered), wheat crop had highest water productivity of 0.60 kg/m³ (WP), followed by rice with 0.5 kg/m³, and cotton with 0.42 kg/m³. In terms of economic value (dollar per unit of water delivered), cotton ranked highest at $ 0.5/m³ followed by wheat with $ 0.33/m³ and rice at $ 0.10/m³. The study successfully delineated the areas of low and high WP. An overwhelming proportion (50+%) of the irrigated areas were under low WP for all crops with only about 10% area in high WP.

Keywords: water productivity mapping, biophysical relationship, vegetation indices, evapotranspiration, remote sensing.

1 INTRODUCTION

Considerable increases in land and water productivity have resulted from agricultural intensification using “green revolution” technologies of short season varieties, artificial
nitrogen fertilizer, and irrigation water. The world’s population continues to grow rapidly, at a
time when water resources are heavily utilized and there is a strong emerging likelihood that
water resources will decrease and become more precarious under the impacts of global
climate change. Consequently, a new challenge is to raise total agricultural production using
no more water than at present, and preferably less. Fresh water withdrawals for agriculture
account for nearly 80% of the total water withdrawal from surface water and groundwater [1].
However, competition for water is now arising across sectors as well as within agriculture,
including: (a) increased demands of urbanization, industries, (b) growing more food for
increasing population (globally about 100 million additional population every year), (c) needs
of environmental flows and recreation, (d) growing needs of biofuel crops, (e) increased
calorie intake per capita in emerging economies, and (f) change in food habits of the people
through increased luxury consumption of fruits and vegetables in more mature economies.
The spatial distribution of water in the world is highly uneven, so that water scarcity is more
acute in some regions than others, notably the arid and semi arid tropics. All these factors call
for development of new technologies for better water productivity (more crop per drop).
Increasing water productivity requires a different approach to agricultural management, to
optimize the use of inputs and management whilst at the same time understanding that land
resources are also limited, which means that a simple strategy of increasing land area with
lower yield but higher water productivity is not a solution in most cases.

The first step in improving performance is to understand the levels, distribution and
patterns of water productivity. This will help us to pin-point areas of high and low WP and
analyze the reasons for variability. This in turn, allows diagnosis of the reasons for low water
productivity which can then be tackled through research and improved land and water
management. Commonly water productivity is assessed at plot or field level, or determined
from secondary crop statistics and water supply or water use data, but actual water use
(evapotranspiration) may be unknown [2]. Remote sensing science offers the possibility of
both greater coverage, and greater spatial detail in mapping water productivity, through the
use of emerging techniques to map and model crop growth and water use, through synoptic
coverage over large areas at regular time intervals. Remote sensing data is now available in
multiple spatial, radiometric and spatial resolutions.

The main goal of this research was to develop methods for WPM using remote sensing
data at various spectral, spatial, and radiometric resolutions. The focus was on irrigated areas.
Specific objectives include: (a) developing methods and protocols for WPMs using remote
sensing data of various resolutions, (b) extrapolating (up-scaling) using the best models to
understand WP variations over space and time; and (c) studying accuracies and errors
involved in WP across scales (or resolutions), radiometry, and bandwidth.

2 METHODS

2.1 Definition of water productivity

Water productivity (WP) is defined as the kilogram of yield produced/m³ of water depleted by
the crop or, alternatively, as value in dollar of yield produced/m³ of water depleted [3].

\[
WP (kg/m^3) = \frac{\text{Yield (kg/m² or kg/pixel) or economic value ($)}}{\text{Water use or ET}_{\text{actual}} (m^3/m^2 \ or \ m^3/pixel)}
\]

Where, \( \text{ET}_{\text{actual}} (m^3) = \text{ET}_{\text{fraction}} \) (dimensionless) * \( \text{ET}_{\text{potential}} (m^3) \)
2.2 Study area

The study area was selected after discussions with local experts in the Syr Darya river basin in Central Asia (Fig. 1). The area called Galaba was selected because it represents the irrigated areas of the entire Syr Darya river basin well, in terms of the following characteristics. Cotton, wheat and rice are the main crops grown in the basin. Cotton accounts for nearly 55 percent of sown area and is the dominant crop. Wheat was the second-most favored crop, covering nearly 30 percent of the area, but it cannot be grown at the same time as cotton because cotton planting has to be completed before wheat can be harvested. As a result many units adopt a two-year rotation system, planting wheat after cotton and leaving the field fallow, planting maize or another short-growing crop after the wheat. Small patches of paddy rice and alfalfa are irregularly distributed across the basin and gardens form an important part of every household. The rainfall in Galaba varies between 100 and 200 mm per year. The average temperature is 0-4° Celsius in January and 28-32° Celsius in July.

The irrigation system in this region is one of the most complex man-made water systems in the world [4]. Virtually all the available surface water has been diverted to irrigation and so there is little scope for further expansion of irrigated area to meet the increasing food demand in the region. Increased water productivity (WP) is the preferred option to meet future food demand in this region. The Galaba study area was covered by a Quickbird image with an area of 6575 hectares (ha).

![Fig. 1. Location of study area: a representative site called Galaba in the Syr Darya river basin.](image-url)
Table 1. Characteristics of remote sensing data sets used in this study.

<table>
<thead>
<tr>
<th>Sensor</th>
<th>Resolution</th>
<th>Band range</th>
<th>Irradiance</th>
<th>Revisit</th>
<th>Acquisition dates</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Spatial (m) Spectral (m) Radiometric (bit)</td>
<td>(µm)</td>
<td>(W m²sr⁻¹µm⁻¹)</td>
<td>(days)</td>
<td></td>
</tr>
<tr>
<td>1. Quickbird</td>
<td>0.61 (Panchromatic); 2.44 (Multispectral)</td>
<td>4 11</td>
<td>0.45-0.52</td>
<td>1381.79</td>
<td>5  July 26, 2006, August 3, 2006</td>
</tr>
<tr>
<td>2. IRS-P6-LISS3</td>
<td>23.5 4 10</td>
<td>0.52-0.59</td>
<td>1857.7</td>
<td>24</td>
<td>2006 (June 5, June 15, June 20, July 9, July 14, July 18, August 26, September 24, October 27, November 6), 2007 (April 13, May 26, June 19, July 18)</td>
</tr>
<tr>
<td>3. Landsat ETM+</td>
<td>14.25 (Panchromatic); 28 (Multispectral); and 60 (Thermal)</td>
<td>8 8</td>
<td>0.45-0.515</td>
<td>0.483</td>
<td>16 2006 (April 24, May 10, June 11, July 29, August 14, October 1)</td>
</tr>
<tr>
<td>4. MODIS (MOD09Q1)</td>
<td>250 2 12</td>
<td>0.62-0.67</td>
<td>1528.2</td>
<td>1</td>
<td>2006-2007, Every 8 days Maximum Value Composite (MVC)</td>
</tr>
<tr>
<td>5. MODIS (MOD09A1)</td>
<td>500 36/7* 12</td>
<td>0.62-0.67</td>
<td>1528.2</td>
<td>1</td>
<td>2006-2007, Every 8 days MVC</td>
</tr>
</tbody>
</table>

* Modis 500m (Mod09A1) has 36 bands, but we considered only the first 7
2.3 Acquisition of images at various resolutions or scales

Imagery was acquired at 4 distinct spectral, spatial, radiometric, and temporal resolutions (Table 1). The data consisted of very fine resolution 0.61-2.44 meter resolution Quickbird, 23.5 m IRS Satellite, 250 m and 500 m MODIS imagery.

2.4 Image normalization

The data acquired from different sensors and even the data acquired from same sensor on different dates need to be normalized before they can be compared. Hence, digital numbers (DNs) were converted to absolute units of radiance (W m$^{-2}$ sr$^{-1}$ μm$^{-1}$), then to apparent at-satellite reflectance (%), and finally to surface reflectance (%) after atmospheric correction [5-6].

2.4.1 Quickbird DN to Reflectance

The Radiometric resolution of Quickbird digital number (DN) data is recorded in 11-bit and stored either in 16-bits or down scaled to 8-bits. There were two steps to calculate radiance from DN values. First is to calculate band integrated radiance expressed as:

$$L_{\text{Pixel,Band}} = \text{absCalFactor}_\lambda \times DN_{ij}$$

Where: $L_{\text{Pixel,Band}}$ is band integrated radiance, absCalFactor is absolute calibration factor as is 0.064 for Pan band, 0.016 for blue, 0.014 for green, 0.013 for red and 0.015 for NIR. DN$_{ij}$ is digital number of pixel in row $i$ and column $j$.

The band average radiance can be calculated based on band integrated radiance using equation:

$$L_{\lambda, \text{Pixel,Band}} = \frac{L_{\text{Pixel,Band}}}{\Delta \lambda_{\text{Band}}}$$

Where:

$L_{\lambda, \text{Pixel,Band}}$ is band averaged radiance, $\Delta \lambda_{\text{Band}}$ is effective bandwidth as shown in Table 2.

<table>
<thead>
<tr>
<th>Spectral Bands</th>
<th>Effective bandwidth ((\Delta \lambda_{\text{Band}})) [μm]</th>
<th>Spectral Irradiance (ESUN(\lambda)) [W-m$^{-2}$-μm$^{-1}$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Panchromatic</td>
<td>0.398</td>
<td>1381.79</td>
</tr>
<tr>
<td>Blue</td>
<td>0.068</td>
<td>1924.59</td>
</tr>
<tr>
<td>Green</td>
<td>0.099</td>
<td>1843.08</td>
</tr>
<tr>
<td>Red</td>
<td>0.071</td>
<td>1574.77</td>
</tr>
<tr>
<td>NIR</td>
<td>0.114</td>
<td>1113.71</td>
</tr>
</tbody>
</table>

2.4.2 IRS P6 (Resourcesat-I) DN data to Reflectance

IRS P6 (Resourcesat-I) Linear Imaging Self Scanning (LISS-3) sensor spectral radiance was computed using the following equation:
\[
L_\lambda = \frac{DN_{ij} \times \text{Gain}}{255}
\]

(3)

Where, Gain is radiance gain given in Table 3. The specific Gain setting was given in individual image header file.

<table>
<thead>
<tr>
<th>Gain Setting</th>
<th>Band2</th>
<th>Band3</th>
<th>Band4</th>
<th>Band5</th>
</tr>
</thead>
<tbody>
<tr>
<td>G1</td>
<td>26.609</td>
<td>27.32</td>
<td>31.018</td>
<td>6.903</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>6.944</td>
</tr>
<tr>
<td>G2</td>
<td>18.471</td>
<td>18.179</td>
<td>20.695</td>
<td>3.397</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>3.406</td>
</tr>
<tr>
<td>G3</td>
<td>12.064</td>
<td>15.131</td>
<td>15.757</td>
<td>1.644</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>1.636</td>
</tr>
<tr>
<td>G4</td>
<td>8.988</td>
<td>10.304</td>
<td>10.876</td>
<td>0.767</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>0.752</td>
</tr>
</tbody>
</table>

Table 3. Radiance gain values for IRS-P6 image data.

2.4.3 Landsat-7 ETM+ DN values to radiance and temperature

The ETM+ 8-bit DNs were converted to radiances using the equation [7]:
\[
L_\lambda = \text{gain} \times \text{DN} + \text{offset}
\]

This can also be expressed as:
\[
L_\lambda = \frac{L_{\text{max}} - L_{\text{min}}}{Q\text{Cal}_{\text{max}} - Q\text{Cal}_{\text{min}}} \times (DN - Q\text{Cal}_{\text{min}}) + L_{\text{min}}
\]

(4)

Where, \( Q\text{Cal}_{\text{min}} = 1 \), \( Q\text{Cal}_{\text{max}} = 225 \), \( L_{\text{min}} \) and \( L_{\text{max}} \) are the spectral radiances for each band at DN 1 and 255 (i.e. \( Q\text{Cal}_{\text{min}}, Q\text{Cal}_{\text{max}} \)), respectively. The \( L_{\text{min}} \) and \( L_{\text{max}} \) values (W/m² Sr µm) are found in image header file.

ETM+ Band 6 imagery can also be converted from spectral radiance (as described above) to a more physically useful variable. This is the effective at-satellite temperatures of the viewed Earth-atmosphere system under an assumption of unity emissivity and using pre-launch calibration constants. The conversion formula is:
\[
T = \frac{K_2}{\ln(K_1/L_\lambda) + 1}
\]

(5)

Where, \( T \) is effective at-sensor temperature in degree Kelvin, \( K_1 \) and \( K_2 \) are calibration constants, \( K_1=666.09 \text{ Wm}^{-2}\text{sr}^{-1}\text{µm}^{-1} \); \( K_2=1282.71 \text{ degree Kelvin} \).

A reduction in between-scene variability can be achieved through normalization for solar irradiance by converting spectral radiance, as calculated above, to planetary reflectance or albedo. This combined surface and atmospheric reflectance of the Earth is computed with the following formula [7]:
\[
\rho_p = \frac{\pi L_\lambda d^2}{ESUN_\lambda \cos \theta_s}
\]

(6)

Where \( \rho_p \) is the at-satellite exo-atmospheric reflectance (or top of the atmosphere (TOA) reflectance or apparent reflectance in %), \( L_\lambda \) is the radiance (W m⁻² sr⁻¹ µm⁻¹), \( d \) is the earth sun distance in astronomical units (dimensionless) at the acquisition date [7], \( ESUN_\lambda \) is the mean solar exo-atmospheric irradiance (W m⁻² sr⁻¹ µm⁻¹) or solar flux, and \( \theta_s \) is solar zenith angle in degrees (i.e., 90 degrees minus the sun elevation or sun angle when the scene is recorded as given in the image header file).
2.4.4 MODIS surface reflectance

MODIS is a key sensor on the Terra (EOS AM-1) satellite. The MODIS Land Science Team provides a suite of standard MODIS data products to users, including the 8-day composite surface reflectance product (MOD09A1). There are forty-six 8-day composites in a year, starting with Julian date of January 1 each year. The MOD09A1 data are organized in tile fashion and freely available to the public from the United States Geological Survey EROS Data Center (http://edc.usgs.gov). The MODIS data has gone through a rigorous atmospheric correction scheme based on the 6S radiative transfer code for normalizing molecular scattering, gaseous absorption, and aerosols that affect the top of the atmosphere (TOA) signal [8]. Aerosol effects are known to remain uncorrected even after long compositing periods (e.g., a month) [8], so such effects in 8-day time intervals are significant. MODIS scans the entire Earth's surface every day, acquiring data in 36 spectral bands. Out of the 36 spectral bands, the first 7 bands are used to study vegetation and land surfaces (Table 1).

2.5 Field-plot data

Field-plot data was acquired to correspond with the satellite sensor overpass dates (Table 1 and section 3.3). In all, 911 field-plot data points were gathered and the data consisted of parameters such as wet and dry biomass (kg/m²), crop yield (kg/m²), hyperspectral data from field-based Spectroradiometer, irrigation water applied (m³), and climate data (Table 4). The number of samples and the distribution of the field-plot data points for various crops are also shown in Table 4. The spatial distribution of some of the field-plot data points are illustrated in Fig. 2.

2.5.1 Field experimental sites

Data from the test sites (fields) at different farms (Water User Association-WUA) were gathered for approximately every 15-days interval for the five crops: cotton, wheat, rice, and maize. A total of 911 sample points were chosen for four crops: cotton (580), wheat (175), maize (113), and rice paddy (43). Enough care was taken while selecting the locations of the field trials (replications) to represent field-field variability. Distribution of these points over a cropping season was illustrated for one farm at three distinct resolutions in Fig. 2.

Biophysical parameters were collected throughout the crop growing season and includes Leaf Area Index (LAI) (Fig. 3a), biomass (Fig. 3b), spectral measurements (Fig. 4), and yield (Fig. 6a). The meteorological data includes temperature, relative humidity, vapor pressure, sunshine hours, wind speed, rainfall, and evapotranspiration (ET) from an ET gauge. The meteorological data were collected from the digital weather station installed in the field, as well from two government managed weather stations. Table 4 gives an overview of the data collected.

The time-series average Normalized Difference Vegetation Index (NDVI), dry biomass, and LAI for all the fields and points are plotted together indicates a closer comparable seasonal pattern (Fig. 3). The initial emergence of the plant after 45 days (i.e. till the day 173) indicates a slow growth and low canopy cover. The NDVI and LAI curves steepen from day 173 and reach a peak by day 214, representing the maximum vegetative growth. LAI tends to fall earlier than NDVI (Fig. 3a) and NDVI continues to increase at the peak when LAI saturates and /or leaf senescence begins while NDVI also starts falling soon after the senescence and leaf falling starts at lower canopy. The study shows strong relationship between NDVI and LAI which is supported by previous studies [9-12]. Dry biomass peaks about 40 days after LAI (Fig. 3b). The seasonal spectrums of the crops were also observed using Spectroradiometer. Initial observations indicate a strong relationship between the crop growth stage (moisture, biomass and vigor) and absorption around 970 nm (Fig. 4).
Table 4. Field-plot data collected from field sites. The total sample points collected are 911, of which the crop wise distributions consist of cotton (580), wheat (175), Maize (113) and rice (43).

<table>
<thead>
<tr>
<th>Variable</th>
<th>Temporal basis (days)</th>
<th>Spatial scale</th>
<th>Mean Sample size</th>
<th>Method</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wet biomass (kg/m²)</td>
<td>15 days</td>
<td>1 m²</td>
<td>224</td>
<td>Crop cutting</td>
</tr>
<tr>
<td>Dry biomass (kg/m²)</td>
<td>15 days</td>
<td>1 m²</td>
<td>224</td>
<td>Crop cutting</td>
</tr>
<tr>
<td>Plant Height (mm)</td>
<td>15 days</td>
<td>1 m²</td>
<td>224</td>
<td>Ruler</td>
</tr>
<tr>
<td>Yield (kg/m²)</td>
<td>One time</td>
<td>1 m²</td>
<td>30</td>
<td>Crop cutting</td>
</tr>
<tr>
<td>Field NDVI (ratio)</td>
<td>15 days</td>
<td>1 m²</td>
<td>220</td>
<td>NDVI Camera</td>
</tr>
<tr>
<td>LAI (m²/m²)</td>
<td>15 days</td>
<td>1 m²</td>
<td>224</td>
<td>LAI Meter</td>
</tr>
<tr>
<td>Canopy reflectance (%)</td>
<td>15 days</td>
<td>Point</td>
<td>224</td>
<td>ASD Spectroradiometer</td>
</tr>
<tr>
<td>Irrigation</td>
<td>Each application</td>
<td>Field</td>
<td>4</td>
<td>Weirs /V-notches</td>
</tr>
<tr>
<td>Climate data (Temp., RH., Wind, Rain, Radiation)</td>
<td>30 min</td>
<td>km²</td>
<td>1</td>
<td>Meteorological station and digital weather stations</td>
</tr>
</tbody>
</table>

Fig. 2. Spatial distribution of the field-plot data points in the study area. The spatial distribution of the field-plot data points were shown for: (a) Quickbird, (b) IRS, and (c) MODIS 250-m.
Fig. 3. Seasonal relationship between LAI and NDVI (a) and LAI and Dry biomass (b) plotted for the average values derived from all field points collected during 11 visits roughly at 15 days interval.

Fig. 4. Seasonal vegetation spectra of a cotton field measured roughly at 15 day intervals and some photographs of the corresponding biomass growth.

3 WATER PRODUCTIVITY MAPPING

The three major steps involved in the mapping process were in producing:

a) Crop productivity maps (CPMs; kg/m² or kg/pixel), which involves;
   i. Crop type mapping;
   ii. Spectro-biophysical/yield modeling; and
   iii. Extrapolating the best spectro-biophysical/yield modeling to larger areas using remotely sensed data.
b) Water use (actual ET) maps (WUMs; m$^3$/m$^2$ or m$^3$/pixel)
   iv. Deriving water use maps (or actual ET) through simplified surface energy balance (SSEB) model; and

c) Water productivity maps (WPMs; kg/m$^3$)
   v. Producing water productivity maps by dividing CPMs with WUMs.

3.1 Crop productivity mapping (kg/m$^2$ or kg/pixel)

The crop productivity maps (CPMs) were produced in three steps:

3.1.1 Mapping crop types using remote sensing

It is important to produce water productivity maps (WPMs) that are crop specific. As every crop type has different water needs to produce a kilogram of marketable produce, it is important to delineate and map crop types first. This allows the development of crop specific spectro-biophysical models (section 4.2), which in turn allow assessment of inter- and intra-field variability in land and water productivity.

Crop types were mapped using time-series IRS-P6 data and the single date Quickbird data. Unsupervised classification of the IRS data, and class identification and labeling process [13,14], were used to delineate and map crop types. IRS-P6 and Quickbird offers detailed within-field variability and clearly demarcates the field boundaries of a crop. In order to define clear field boundaries at other resolutions, the crop and field boundaries were digitized manually from the Quickbird imagery. Due to their distinct cropping calendars, all four crops were easily distinguishable.

3.1.2 Spectro-biophysical/yield models

The crop biophysical and yield variables were related to spectral measurements from space. The most commonly used crop variables establishing such relations were the leaf area index (LAI), Wet Biomass (WBM), Dry Biomass (DBM), and grain Yield (YLD). Variation in the reflectance was normally associated with chlorophyll and water contents of the plants [15-16]. Satellite-based radiative indices were good indicator of LAI, which is one of the important parameters in the models. Some were also correlated with photosynthetically active radiation (PAR), which is correlated to the CO$_2$ assimilation [17]. LAI, biomass, and, to some extent, plant height were excellent indicators of the plant growth, condition, and yield [18]. The spectral vegetation indices derived using field-plot data and space-borne sensors were effectively used for rapid assessment and characterization of crop biophysical variables such as biomass, LAI, plant height, and yield [11,19-22]. A Production Efficiency Model (PEM) that estimates crop growth from intercepted photosynthetically active radiation (IPAR) and light use efficiency ($\varepsilon$) was introduced [23,24]. Subsequent studies further improved the model by making $\varepsilon$ a function of temperature, water, and nutrient stress, such as the Carnegie-Ames-Stanford-Approach (CASA) [25-26]. The methodology has been widely used to estimate terrestrial ecosystem net primary production (NPP), global carbon cycle [25-27], and crop production at regional scale [28-30].

During this research, extensive measurements of LAI, biomass and yield were collected during routine field visit at every ~15 days interval (Table 4). These measurements were related to wavebands and indices derived from the satellite sensor data (Table 1). In the past, remote sensing has proved very useful in estimating area and production of cereals and other food crops [6,12,31] and the relationships have improved with the use of modern high-spectral and high-spatial sensors [5,12]. For example, the NDVI was found to correlate with net primary production, biomass, vegetation fraction, and yield [32-37]. Although the results of correlation analysis are purely empirical, they are in agreement with numerous theoretical, experimental, and statistical studies [39]. In this research, spectro-biophysical models were
run using statistical analysis system (SAS) software package. Biophysical and yield data (Table 2) gathered during routine field visits were related to spectral data obtained from various sensors (Table 1). The type of models included: (a) linear, (b) multiple linear, (c) non-linear power, and (d) non-linear exponential.

3.1.3 Extrapolation of models to spatial domain

One of the biggest strengths of remote sensing lies in the observation of the entire landscape rather than just few points [40]. With good understanding of the relationships between crop variables and spectral reflectivity and/or indices it is possible to extrapolate the understanding gained through models to larger areas by utilizing the best models of specific crops and specific variables (developed in section 4.1.2) to specific crops (delineated in section 4.1.1).

Extrapolation, for example, will involve taking the best cotton yield predictor model developed in section 4.1.2 based on point data and applying the same to all cotton growing areas that has been delineated using the remotely sensed data.

3.2 Mapping Evapotranspiration

Water used by crops was determined by computing actual evapotranspiration (ET\text{actual}) from remote sensing and non-remote sensing approaches. The ET derived from different surfaces varies with different methods [41,42,43], which leads to inconsistency and uncertainty in ET estimation. The Food and Agriculture Organization (FAO) Penman–Monteith equation—with the parameterization as elaborated by Allen et al. (44) has become the de facto standard method to estimate reference ET (45) for point-level ET estimation using climate data collected at field scale. The point based ET measurements from the field and weather stations data have been integrated with remote sensing images to spatially extrapolate from pixel level to basin scale [46;47].

However, the water used by crops is best determined using surface energy balance algorithms that are primarily dependant on remotely sensed data. The potential of remote sensing in estimating the ET [48-51] is well established using Surface Energy Balance Algorithm (SEBAL) [52-53], the modified SEBAL, and mapping ET with high resolution and internalized calibration (METRIC) [54]. Gabriel and Verdin [55-56] and Gabriel et al [57] recommended a Simplified Surface Energy Balance (SSEB) model using remote sensing. The SSEB approach was adopted in this study to facilitate rapid computation of water use over large areas in a rapid time-frame. The SSEB model is defined as follows:

\[
\text{ET}_{\text{actual}} (\text{m}^3/\text{m}^2 \text{ or } \text{m}^3/\text{pixel}) = \text{ET}_{\text{fraction}} \times \text{ET}_{\text{reference}}
\]

Water used by crops, the ET (expressed in m³/ha or mm/m²) was determined from remote sensing by calculating the ET\text{actual} based on the following steps:

- \text{ET}_{\text{fraction from Landsat ETM+ thermal data}}. The principal assumption in SSEB model that the latent heat flux (ET\text{actual}) varies linearly between the “hot” and “cold” pixels. The fraction of ET was estimated from the land surface temperature (LST) of “hot” and “cold” pixels using following formula:

\[
\text{ET}_{\text{fraction}} = (\text{Thot} - T) / (\text{Thot} - \text{Tcold})
\]

Where: ET\text{fraction} was the fraction of ET; T is the LST of any pixel; Thot and Tcold are the LST of “hot” and “cold” pixels respectively, selected inside the study area. The ET\text{reference} was calculated from weather station data using Penman-Monteith equation [44]. The final ET value for each pixel was determined by multiplying ET\text{fraction} with ET\text{reference}, which finally gives ET\text{actual}. 

\[
\text{ET}_{\text{actual}} (\text{m}^3/\text{m}^2 \text{ or } \text{m}^3/\text{pixel}) = \text{ET}_{\text{fraction}} \times \text{ET}_{\text{reference}}
\]
3.3 Water productivity mapping

3.3.1 Producing water productivity maps (WPMs)

The WPMs were produced by dividing the crop productivity map (CPMs; section 4.1) with water use map (WUMs; section 4.2). The WPMs were defined as:

\[
\text{Water Productivity Maps (kg/m}^3\text{)} = \frac{\text{Yield (kg/m}^2\text{ or kg/pixel) or economic value (})}{\text{Water use (m}^3\text{/m}^2\text{ or m}^3\text{/pixel) }}
\]

(8)

4 RESULTS AND DISCUSSIONS

4.1 Crop productivity mapping

4.1.1 Crop type maps at various resolutions

The results of the attempts to map the crop type maps using remotely sensed data at 4 spatial resolutions, Quickbird (2.4m), IRS P6 (23.5m), and MODIS 250m/500m MOD09Q1, are shown in Fig. 5. It was possible to delineate crop types using the Quickbird (Fig. 5a) and IRS (Fig. 5b) data. At 250m resolution (MODIS) it is only possible to establish the dominant crop in the mix (Fig. 5c). Using the MODIS 500m data, only irrigated areas were mapped, without separating any crop types or crop dominance (Fig. 5d). The ability of satellite sensor data to map crop types and/or their dominance at 4 spatial resolutions is summarized in Table 5.

Table 5. The ability to map irrigated crop types and their dominance using satellite sensor data at 4 spatial resolutions.

<table>
<thead>
<tr>
<th>Aggregated types</th>
<th>LULC Quickbird (2.4m)</th>
<th>IRS-P6 (23.5m)</th>
<th>MODIS (250m)</th>
<th>MODIS (500m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cotton</td>
<td>Yes</td>
<td>Yes</td>
<td>zero</td>
<td>zero</td>
</tr>
<tr>
<td>Wheat</td>
<td>Yes</td>
<td>Yes</td>
<td>zero</td>
<td>zero</td>
</tr>
<tr>
<td>Rice paddy</td>
<td>Yes</td>
<td>Yes</td>
<td>zero</td>
<td>zero</td>
</tr>
<tr>
<td>Cotton dominant</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>zero</td>
</tr>
<tr>
<td>Rice dominant</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>zero</td>
</tr>
</tbody>
</table>

4.1.2 Modeling crop growth and yield (Spectro-biophysical/yield models)

The spectro-biophysical/yield models were developed using Quickbird and IRS-P6 data for cotton, wheat, and maize (Table 6). The crop variables modeled were wet and dry biomass (kg/m2), LAI (m2/m2), and grain yield (ton/ha). The best models to determine variables such as biomass, LAI, and yield were highly significant and explained around 80 percent variability for IRS-P6 and 70 percent variability for Quickbird data. Due to the non availability of time-series images, Quickbird models were only used for biomass. Most of the variables were modeled with IRS-P6 data due to good temporal coverage for entire growing season. The best IRS-based models for cotton were the wet biomass, dry biomass, LAI, and yield with 72-83 percent variability (Table 6). The best fit models for the wheat and maize are the LAI, wet biomass, and yield (Table 6). Spectro-biophysical/yield models could not be developed from MODIS data due to its inability to separate crop types.
Fig. 5. Crop types mapped at various resolutions. Crop types mapped using: (a) Quickbird 2.4m, (b) IRS P6 (Resourcesat1, Liss3) 23.5m, (c) MODIS 250m, and (d) MODIS 500m. The classification schemes clearly indicate that the number of classes reduced with increasing pixel size due to aggregation.

Table 6. The best spectro-biophysical/yield models using Quickbird 2.44m and IRS 23.5m data.

<table>
<thead>
<tr>
<th>Sensor</th>
<th>Crop</th>
<th>Variable</th>
<th>Equation</th>
<th>$r^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>IRS</td>
<td>Cotton</td>
<td>Wet biomass</td>
<td>$y=71.18*(x)^{1.36}$</td>
<td>0.83</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Dry biomass</td>
<td>$y=51.59*(x)^{4.86}$</td>
<td>0.82</td>
</tr>
<tr>
<td></td>
<td></td>
<td>LAI</td>
<td>$y=10.37*(x)^{1.916}$</td>
<td>0.73</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Yield</td>
<td>$y=5.156*x-0.964$</td>
<td>0.75</td>
</tr>
<tr>
<td>IRS</td>
<td>Wheat</td>
<td>LAI</td>
<td>$y=0.005*(x)^2-0.509*(x)+7.175$</td>
<td>0.80</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Yield</td>
<td>$y=6.192*x-0.47$</td>
<td>0.66</td>
</tr>
<tr>
<td>IRS</td>
<td>Maize</td>
<td>Wet biomass</td>
<td>$y=34.664*(x)^{4.136}$</td>
<td>0.87</td>
</tr>
</tbody>
</table>

Note: x = NDVI

4.1.3 Extrapolation of models to spatial domain and deriving crop productivity maps (CPMs)

The best models (Table 6) were used on the relevant images (see image list in Table 1) to extrapolate and derive crop characteristics such as grain yield, wet biomass, dry biomass, and LAI. The result of extrapolation was shown for cotton yield (ton/ha) using IRS data (Fig. 7). The extrapolation was possible as a result of the good understanding we had through model development (Table 4) and delineation of crop types (section 4.1.1 and 5.1.1). The extrapolated areas (Fig. 7) show spatial variability within a crop derived for various crop
variables. These CPMs were one of the key parameter in understanding within and between-field variability leading to finding appropriate site specific solutions.

![Graphs showing](image)

**Fig. 6.** The relationship between spectral and biophysical variables for the spaceborne satellite sensors data and field-plot data illustrated taking: (a) cotton yield versus IRS P6 NDVI and (b) cotton wet biomass versus Quickbird NDVI.

![Map of Crop Productivity](image)

**Fig. 7.** Crop productivity map (CPM). CPM illustrated using a IRS P6 image by extrapolation of the best crop specific spectro-biophysical/yield models and by using crop type maps (Fig.5).

### 4.2 Water use (actual ET) mapping (m³/m² or m³/pixel)

The water use by crops was determined by ET$_{actual}$ computations. The simplified surface energy balance (SSEB) model algorithm was used to determine ET$_{actual}$. First, it required computation of evaporative fraction, which was then multiplied by ET$_{reference}$ to obtain the ET$_{actual}$.
The evaporative fraction (ET fraction) was determined using the Landsat-7 ETM+ thermal imagery. ET reference was computed using FAO Penman-Monteith formula. The ET actual was then computed by multiplying ET fraction * ET reference and was computed for every month. Monthly ET actual were then cumulated, taking the cropping calendar into consideration. This lead to an accumulated ET actual for the entire crop growing season (see an example for cotton crop in Fig. 8).

4.2.1 Relationship between ET actual versus NDVI

The NDVI showed strong relationship with ET actual derived from Landsat-7 ETM+ and climate data using SSEB model (Fig. 9). We have presented this relationship to show potential of vegetation indices in mapping ET. The approach requires more research for individual crops and by using larger sample size of data.

The IRS P6 derived NDVI values of the cotton crop were correlated with ET fraction from ETM+ images. Platonov et al. [59] have reported similar agreement when compared Landsat-7 ETM+ NDVI values with Landsat-7 ETM+ derived ET fraction. The daily water consumption by field crops were calculated by multiplying ET reference with ET fraction with an assumption that ET fraction derived for the day for which the image was acquired remains constant throughout the month for a given crop. Second, crop wise water use per pixel was determined on monthly basis leads to entire growing season. The results are finally presented in thousands m³/ha of water used for the entire study area.

Fig. 8. Water use maps (WUMs). WUMs or ET actual of cotton crop for the entire crop growing season.

4.3 Water productivity maps (WPMs)

Finally, water productivity maps were produced for every crop by dividing the crop productivity maps (CPMs; section 5.1) with water use maps (WUMs; section 5.2). The WPMs produced separately for each crop were put together and presented in Fig. 11.

The water productivity (WP; kilogram of yield per m³ of water delivered or kg/m³ or economic value, $/m³) computed using remote sensing for three crops were presented in Table 7. From the results, wheat has the best physical WP, followed by rice, and cotton.
However, this pattern is reversed when considered in terms of economic value rather than yield by weight as numerator. Cotton then ranks first with an average market value of $0.5/m^3$ followed by wheat, and rice of $0.3/m^3$, and $0.1/m^3$ respectively. The water productivity map for the cotton crop was produced with varying field variability (Fig. 10). An overwhelming proportion cotton fields were under low WP with only about 12% area in high WP.

Fig. 9. NDVI relationship with ET\textsubscript{actual}. IRS P6 derived cotton NDVI for the month of July, 2006 compared with ET\textsubscript{actual} derived using SSEB model from the Landsat7 ETM+ for the July, 2006.

Fig. 10. Water productivity map (WPMs) for 3 crops using IRS P6 data. Overwhelming proportion (50%+) of all 3 crops were under low WP, with only about 10% area in high WP.
Table 7. Water productivity of the three selected crops determined using IRS P6 and field-plot data.

<table>
<thead>
<tr>
<th>Crop type</th>
<th>Area (ha)</th>
<th>Seasonal Crop ET&lt;sub&gt;actual&lt;/sub&gt; (m&lt;sup&gt;3&lt;/sup&gt;/ha)</th>
<th>Grain Yield (kg/ha)</th>
<th>Water Productivity based on ET&lt;sub&gt;actual&lt;/sub&gt; (kg/m&lt;sup&gt;3&lt;/sup&gt;)</th>
<th>Water Productivity based on average market value in Asia ($/m&lt;sup&gt;3&lt;/sup&gt;)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cotton</td>
<td>3783</td>
<td>3050</td>
<td>1275</td>
<td>0.42</td>
<td>0.50</td>
</tr>
<tr>
<td>Wheat</td>
<td>1571</td>
<td>3100</td>
<td>1850</td>
<td>0.60</td>
<td>0.33</td>
</tr>
<tr>
<td>Rice paddy</td>
<td>313</td>
<td>6650</td>
<td>3320</td>
<td>0.50</td>
<td>0.10</td>
</tr>
</tbody>
</table>

5 CONCLUSIONS

This paper demonstrated methods and protocols required for producing water productivity maps using remote sensing data at various resolutions (or scale): (a) Quickbird 2.44 m, (b) IRS 23.5 m, (c) Landsat7 ETM+ thermal data, (d) MODIS 250m data, and (e) MODIS 500m data.

First, crop productivity maps (CPMs; kg/m<sup>2</sup> or kg/pixel) were computed and involved: (i) crop type mapping using remote sensing, (ii) spectro-biophysical/yield modeling involving parameters measured in the field and relating them to spectral wavebands and indices, and (iii) extrapolation of models to larger spatial domains using remote sensing. Crop types were successfully separated by Quickbird and IRS data, but not by MODIS 250m or 500m data. But it was possible, at times, to map crop dominance using MODIS250m and irrigated crops using MODIS 500m data.

Second, water use maps (WUMs; m<sup>3</sup>/m<sup>2</sup>) were determined through thermal data of Landsat-7 ETM+ using simplified surface energy balance (SSEB) model and summing up water use determined from time-series imagery. Results showed that, water use of cotton crop was 3050 m<sup>3</sup>/ha whereas wheat used 3100 m<sup>3</sup>/ha, and rice 6650 m<sup>3</sup>/ha.

Third, water productivity maps (WPMs) were produced by dividing crop productivity maps with water use maps. Wheat with 0.60 kg/m<sup>2</sup> had the best water productivity (WP), followed by rice with 0.5 kg/m<sup>2</sup>, and cotton with 0.42 kg/m<sup>3</sup>. In terms of economic value of WP, cotton crop earned about the $ 0.5/m<sup>3</sup> followed by wheat with $ 0.33/m<sup>3</sup>, and rice with $ 0.10/m<sup>3</sup>. The study has successfully delineated the areas of low and high WP for 3 crops (Figure 10). An overwhelming proportion (50%+) of the irrigated areas were under low WP with only about 10% area in high WP. These results imply that there is significant scope for increasing WP for growing more food to feed the ballooning populations in the coming decades without having to increase allocations of croplands and/or water.

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References


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