

# Journal of Nanophotonics

[SPIDigitalLibrary.org/jnp](http://SPIDigitalLibrary.org/jnp)

## **Medium-wavelength infrared gas sensing with electrochemically fabricated porous silicon optical rugate filters**

Brian H. King  
Michael J. Sailor

# Medium-wavelength infrared gas sensing with electrochemically fabricated porous silicon optical rugate filters

Brian H. King and Michael J. Sailor

University of California, San Diego, Department of Chemistry and Biochemistry,  
9500 Gilman Drive, M/C 0358, La Jolla, California 92093-0358  
[msailor@ucsd.edu](mailto:msailor@ucsd.edu)

**Abstract.** Porous silicon optical rugate filters are electrochemically fabricated to display reflectance peaks in the medium-wavelength infrared (MWIR) region from 4 to 8  $\mu\text{m}$ . Etching conditions are adjusted to create filters with single and multiple infrared reflectance peaks overlapping specific infrared chemical absorbance bands. Additional infrared reflectance peaks are designed into the structures to provide internal optical reference channels. Samples containing optical reflectance features matching the absorbance band of  $\text{CO}_2$  at  $2350\text{ cm}^{-1}$  are used to demonstrate gas sensing with optical filters, and a structure with a photonic stop band tuned to match the infrared absorbance band of the P=O functional group, found in G-series chemical warfare agents, is fabricated. With adequate electrolyte replenishment, the calibrated etch conditions generated reproducible spectral band features even for relatively long etch durations. This work represents the first example of a porous Si spectral filter prepared to match specific spectral features of molecules in the MWIR (“fingerprint”) region. © 2011 Society of Photo-Optical Instrumentation Engineers (SPIE). [DOI: [10.1117/1.3558740](https://doi.org/10.1117/1.3558740)]

**Keywords:** porous silicon; optical filters; rugate filters; spectral imaging.

Paper 10062SSPRR received Sep. 28, 2010; revised manuscript received Dec. 13, 2011; accepted for publication Dec. 15, 2010; published online Mar. 17, 2011.

## 1 Introduction

Porous silicon optical films produced by the electrochemical etching of silicon<sup>1</sup> present an attractive means of creating a film with multiple tunable optical features. The current density applied during the etch process determines the porosity-depth profile and the resulting refractive index profile of the film with depth, allowing a variety of optical structures to be programmed into the material. Structures including Bragg stacks,<sup>2,3</sup> Fabry–Pérot layers,<sup>2</sup> and single and multiple stopband rugates<sup>3,4</sup> have been widely produced and applied to gas sensing in the visible and near-infrared (NIR) region of the spectrum. Rugate structures contain a sinusoidal refractive index variation with depth. Multiple sinusoids can be combined into composite profiles that display stop bands corresponding to each component frequency.<sup>4,5</sup>

This work demonstrates the use of an electrochemically prepared porous Si-based optical filter to optically sense target molecules at medium-wave infrared (MWIR) wavelengths by matching the reflectance spectrum of the porous Si layer to the infrared absorption bands of target molecules ( $\text{CO}_2$  and P=O species in this work). The  $\text{CO}_2$  detector uses a rugate filter tuned to match the principal  $\nu\text{CO}_2$  stretching mode of carbon dioxide at  $2350\text{ cm}^{-1}$ .<sup>6,7</sup> Typically, spectral imaging systems detect  $\text{CO}_2$  at NIR wavelengths like  $2.05\text{ }\mu\text{m}$  due to the availability of sensitive detectors in this wavelength range,<sup>8</sup> but as a proof of principle the  $4.2\text{ }\mu\text{m}$  MWIR

absorption band was utilized here. A composite filter based on the superposition of two sinusoid frequencies was also constructed to create a structure that incorporates a tunable reflectance reference channel. In order to demonstrate the ability to fabricate infrared reflection features at the edge of the long-wave infrared region, a filter was constructed with an optical peak at  $1250\text{ cm}^{-1}$  ( $8\text{ }\mu\text{m}$ ), the wavelength of the P=O bond vibration in the G-series chemical warfare agents soman, sarin, tabun, and VX.<sup>9,10</sup>

In recent years, porous silicon structures prepared as optical rugates in the infrared region of the spectrum have primarily focused on the near infrared, particularly at telecommunications wavelengths for applications such as broadband mirrors and switches.<sup>3,11,12</sup> Some sensing work at NIR wavelengths has been performed, with Chapron applying NIR rugates in the  $1\text{--}3\text{ }\mu\text{m}$  region to directly detect liquid analytes with the porous matrix.<sup>13</sup> Because NIR structures require shorter spacing of the dielectric layers and, thus, thinner films than those required for medium and long wave infrared filters, they are less affected by electrochemical fabrication issues of electrolyte diffusion and depletion that can occur at long etch times. Typical methods to prepare MWIR filters, such as chemical vapor deposition,<sup>14</sup> glancing angle deposition,<sup>15</sup> and thermal evaporation<sup>16,17</sup> are slow and costly.

MWIR optical structures pose additional fabrication challenges, but there is a significant need for infrared hyperspectral imaging systems and filters for two-dimensional infrared imaging that make up the low-cost, rapid electrochemical fabrication method used to prepare porous Si desirable. Recently, Ishikura et al. fabricated MWIR porous silicon structures at  $5\text{--}10\text{ }\mu\text{m}$ , demonstrating the ability to create broadband high-pass filters,<sup>18</sup> and Lo and Murphy have demonstrated fabrication of rugate filters with broad stop bands at terahertz frequencies.<sup>19</sup> In contrast, the aim of this work is to create narrowband spectral features that overlap the vibrational bands of gas-phase molecules and to demonstrate the application of these structures to free-space infrared gas sensing using a reflectance-mode filter with a MWIR detector.

The large planar surface area of the porous Si filter ( $1.2\text{ cm}^2$  in this study) motivates their application as optical filters for 2-D infrared imaging, because the filters are sufficiently large enough to cover the imaging field. In the NIR, 2-D imaging has been used for applications including counterfeit pharmaceutical detection<sup>20</sup> and hyperspectral microscopy. In the MWIR, imaging is of interest for satellite remote imaging<sup>21</sup> and remote sensing,<sup>22</sup> as well as military applications in airborne surveillance, target detection and tracking, and thermal imaging. The ability to acquire 2-D infrared images was developed in the 1970s, and a variety of detection materials, such as vanadium oxide bolometers and barium strontium titanate detectors, have employed.<sup>23</sup> In the past decade, quantum-dot infrared photodetectors<sup>24</sup> (QDIPs) and quantum-well infrared photodetectors (QWIPs) have enabled cameras with megapixel resolution.<sup>25</sup> Ordered photonic structures have even been used for infrared detection,<sup>26</sup> but the work presented here aims not to capture infrared photons with porous Si photonic crystals but rather to complement existing imaging detectors with a passive porous Si filter element. Porous Si can be tailored to exhibit sharp spectral features.<sup>27</sup> In contrast, recent developments with voltage tunable multiband infrared focal plane arrays using MEMS technology<sup>23</sup> to create tunable infrared filters has resulted in broadband structures that are not suitable to sensing specific chemical species by matching molecular vibrational absorption bands. This work represents the first example of a porous Si spectral filter prepared to match specific spectral features of molecules in the MWIR (fingerprint) region.

Although the ability of the filters to restrict specific optical wavelengths makes them an attractive material to couple with broadband infrared detectors [such as a forward-looking infrared camera], a narrowband, high-resolution Fourier-transform infrared (FTIR) spectrometer was employed in the present study in order to quantify the spectral characteristics of the porous Si filters. FTIR is widely used for sensing chemical agents<sup>28</sup> and forensic chemical imaging, with a single scan providing a spectrum analogous to a single pixel in a hyperspectral infrared imaging system.<sup>29</sup>

## 2 Experimental Setup

### 2.1 Fabrication of Optical Structures

Porous Si samples were prepared from single-crystal, (100)-oriented highly boron-doped *p*-type Si (Siltronix, Archamps, France, 0.92 mΩ cm resistivity) by electrochemical etching in a 3:1 v:v solution of aqueous hydrofluoric acid (HF) to ethanol (49% hydrofluoric acid from Fisher Scientific, Inc., Pittsburgh, PA, USA). Etching was performed in a Teflon<sup>®</sup> cell with a platinum mesh counter electrode and a galvanostat (Kepco, Inc., Flushing, NY, USA, BOP 50–4D) under computer control (LabView, National Instruments, Austin, TX, USA). Single- and composite-frequency rugate etches were fabricated with a current waveform varying between 25 and 100 mA/cm<sup>2</sup>, applied nominally for 45 cycles with other sinusoid conditions as indicated. Fresh HF was introduced to the etch cell during electrochemical fabrication by replacing 1.5 mL of the 3:1 etch solution at 5-min intervals. Lifted-off porous films for use in FTIR transmission mode were achieved by detaching the porous layer from the bulk Si wafer with an electropolishing current of 2.7 mA/cm<sup>2</sup> for 5 min in a 3.3% HF:ethanol solution. Rugate etch currents varied as a function of time *t*, according to

$$I(t) = \frac{\sum_{i=1}^n I_i}{n}, \quad (1)$$

where

$$I_i(t) = I_{\min} + \left[ \frac{I_{\max} - I_{\min}}{2} \right] \left[ \sin \left( \frac{2\pi t}{p_i} \right) + 1 \right], \quad (2)$$

where  $I_{\max}$  and  $I_{\min}$  are the high and low currents, and  $p$  is the period of component  $i$  in seconds. For single-frequency rugates,  $n = 1$ . The composite rugate described later contained  $n = 2$  components with periods  $p_1$  and  $p_2$ .

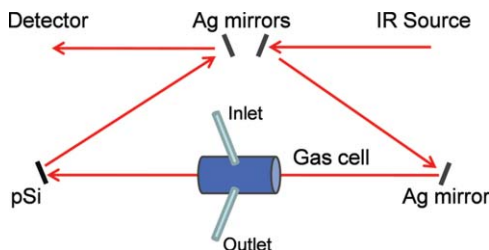
### 2.2 Gravimetric Determination of Porosity

Samples were weighed before etching ( $m_1$ ), after etching ( $m_2$ ), and after dissolving the porous layer with a 0.1-M basic solution of KOH in water and rinsing with ethanol ( $m_3$ ). The following equation was used to determine the porosity:<sup>30</sup>

$$\text{Porosity} = \frac{m_1 - m_2}{m_1 - m_3}. \quad (3)$$

### 2.3 Infrared Spectroscopy

Spectra were recorded with a Thermo Scientific Nicolet 6700 FTIR with an MCT/A detector and KBr beam splitter using a resolution of 2 cm<sup>-1</sup> and an average of 128 scans. Attenuated total reflectance (ATR) spectra were acquired with a smart iTR diamond accessory. Transmission-mode spectra were acquired by mounting the lifted-off porous Si film between two KBr circular plates (Koch Crystal, Elyria, OH, USA) and placing the assembly on a transmittance accessory stage normal to the infrared beam. Reflectance-mode spectra were acquired with a beam-deflector setup as pictured in Fig. 1 and with filters that were not lifted off from the bulk underlying Si. Four Ag mirrors (Thorlabs, Newton, NJ, USA), mounted on posts and positioned at a specular angle of 12.5 deg, diverted the beam path through a gas sample cell. The 2.5-in-long glass gas cell was positioned in the beam path as depicted and used KBr windows and had Swagelok input and output ports. Reference spectra were taken by replacing one mirror, on the detector side of the gas cell, with polished Si. Sample spectra were taken by replacing the



**Fig. 1** Schematic view of the reflectance-mode gas-sensing configuration used. The source and detector are from a conventional FTIR instrument. Silver mirrors divert the beam (arrows) through a gas cell with KBr windows. The porous silicon optical structure (pSi) is mounted at one of the beam-deflection locations, as pictured. A reference spectrum is acquired with a polished silicon chip mounted in the pSi location.

polished Si with a porous Si sample. A flow of  $\sim 2$  L/min of nitrogen, measured with a mass flow controller (Alicat Scientific, Tucson, AZ, USA) was passed through the gas cell. Spectral acquisitions with  $\text{CO}_2$  were taken by first purging the cell with a 2-L/min flow of  $\text{CO}_2$  for 5 min, with continuous flow during sampling.

## 2.4 Effectical Optical Thickness Determination

Reflectance spectra of the samples in the visible region were taken across 530–1200 nm with a CCD spectrometer (Ocean Optics, Dunedin, FL, USA, USB4000) and a tungsten-halogen light source (Ocean Optics LS-1) connected with a Y-branch bifurcated optical fiber. The common end of the bifurcated fiber was focused with an objective lens to a  $2\text{-mm}^2$  spot size and positioned normal to the porous silicon sample surface. A routine using a fast Fourier transform (FFT) of the optical interference fringes in the visible between 850 and 1000 nm was used to determine the effective optical thickness (EOT) (2 nL) of the layers.<sup>31</sup>

## 2.5 Scanning Electron Microscopy

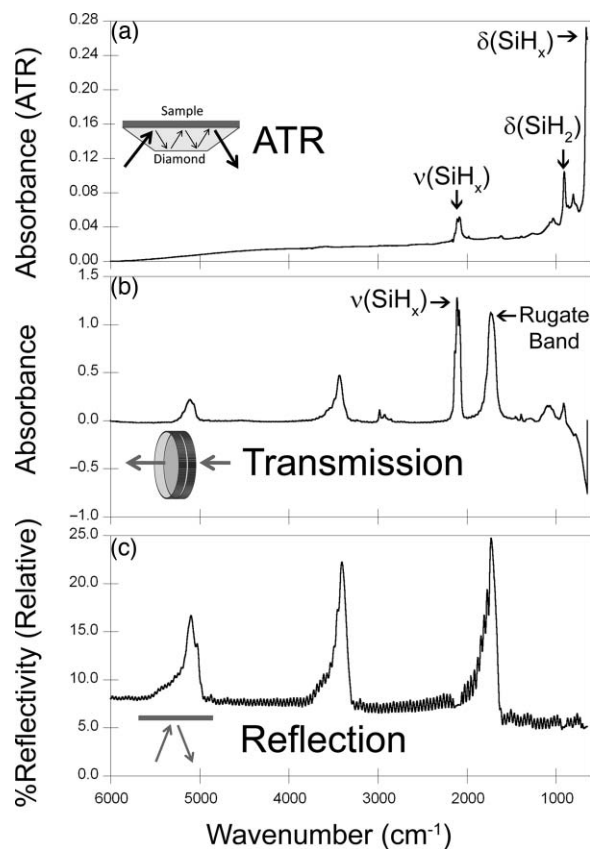
Porous silicon layer thickness was determined by cutting and imaging cross sections of the filters with an FEI XL30 SFEG scanning electron microscope (SEM) in ultra high-resolution mode with a through lens detector at 10 kV without prior metallic sputtering of the sample.

## 3 Results and Discussion

### 3.1 Porous Si Rugate Filters with Medium-Wavelength Infrared Spectral Features

A comparison of spectra from three FTIR acquisition configurations for a filter with a sinusoidal current-time waveform period of  $p = 60$  s is shown in Fig. 2. In all configurations, spectral bands corresponding to the filter material are observed. The filters in this study were designed with resonant peaks outside of the bands corresponding to the Si–H vibrational signatures of the freshly prepared filters. Oxidation of the filters by aging in air will introduce spectral bands corresponding to Si–O and Si–OH bonds that must also be avoided. Spectra obtained in the ATR configuration clearly exhibit features of the fresh Si–H surface, with  $\nu(\text{SiH}_x)$  stretches at  $2112$  and  $2087\text{ cm}^{-1}$ ,  $\delta(\text{SiH}_2)$  at  $907\text{ cm}^{-1}$ , and  $\delta(\text{SiH}_x)$  at  $623\text{ cm}^{-1}$ . No rugate stop band feature is visible under ATR due to the limited depth of penetration of the infrared beam into the filter layer relative to the physical thickness of the rugate cycles.

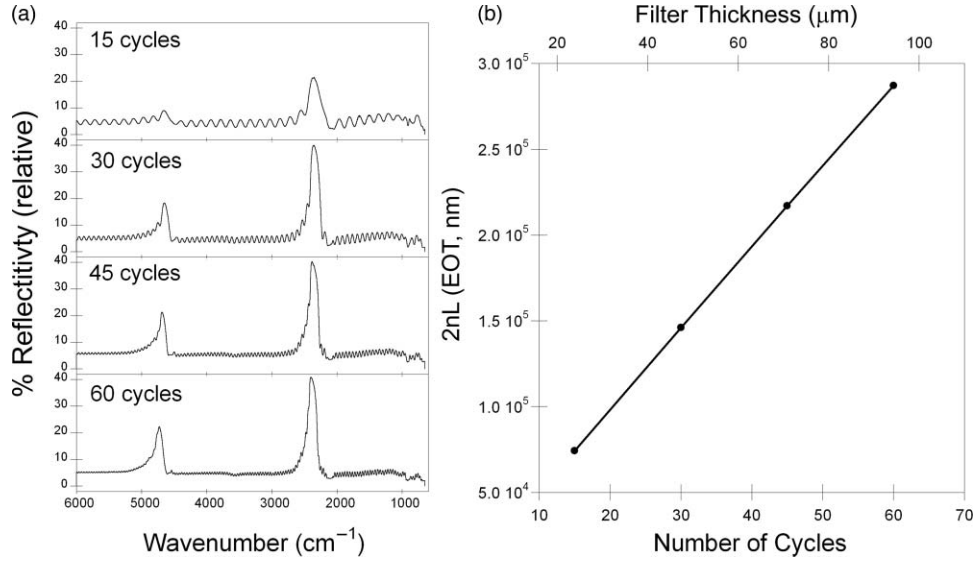
In the transmission configuration, the  $\nu(\text{SiH}_x)$  stretching vibration is very strong, since the light is absorbed in that band as it passes through the optical film. The principal rugate band



**Fig. 2** Comparison of three FTIR acquisition modes and resulting spectra for an infrared rugate optical structure with a sinusoid etching wave period of 60 s. (a) Attenuated total reflectance. (b) The optical structure was lifted off from the bulk and the spectrum acquired in transmission mode. (c) Reflection-mode interrogation using the beam diversion configuration in Fig. 1. The percent reflectivity is relative to a polished Si reference sample.

at  $1715\text{ cm}^{-1}$  is observed, as well as higher order harmonics at  $2/\lambda$  and  $3/\lambda$ .<sup>4</sup> If desired, these higher order harmonics may be suppressed by creating filters with a sinusoidal modulation of the logarithm of the refractive index  $n$  with depth<sup>3,18</sup> rather than a direct sine variation of  $n$ . Here, the  $2/\lambda$  band was desired and utilized as an optical reference channel. The thickness of the filter balances a trade-off between increasing the number of sinusoid repetitions to reduce thin-film interference fringes and increasing the material's absorbance in the Si-H bands outside of the desired rugate spectral position.

To sense absorbing molecules in the beam path, a reflection rather than transmission configuration is desirable. In reflection mode, an absorbing gas is sensed as a reduction in peak reflectivity, while in transmission mode the absorbing gas results in a slight decrease in the already low filter transmittance of the rugate band. The spectrum in Fig. 2 obtained in the reflection configuration clearly exhibits the rugate reflection band as well as higher order harmonics at  $2/\lambda$  and  $3/\lambda$ , with the Si-H stretches of the material's absorbance appearing as reductions in the reflectivity at  $\sim 2100\text{ cm}^{-1}$ . Thin-film interference fringes are present due to reflections from the top and bottom interfaces of the optical structure, where the bottom interface consists of the porous Si layer and bulk silicon. Despite mounting the porous Si sample at a 15-deg angle of incidence, the center wavenumber of the rugate band at  $1742\text{ cm}^{-1}$  in the reflectance configuration was only slightly lower than its appearance at  $1730\text{ cm}^{-1}$  in the transmission configuration, where the filter was normal to the incident beam. This is not surprising



**Fig. 3** (a) Effect of the number of sine wave cycles on the reflectivity spectrum, for an optical structure with a period of 43.7 s. (b) Linear relationship between the effective optical thickness ( $2n_{\text{avg}}L$ , determined from the interference fringes apparent in the visible portion of the reflectance spectrum), and the number of sine wave cycles.

because, for an incident angle  $\theta_0$ , the wavelength of the peak at an angle  $\theta$  relative to its location at normal incidence ( $\lambda_0$ ) is given by:<sup>12</sup>

$$\lambda_\theta = \lambda_0 \cos(\theta_a) = \lambda_0 \left( 1 - \frac{\sin^2 \theta_0}{n_{\text{avg}}^2} \right)^{1/2}, \quad (4)$$

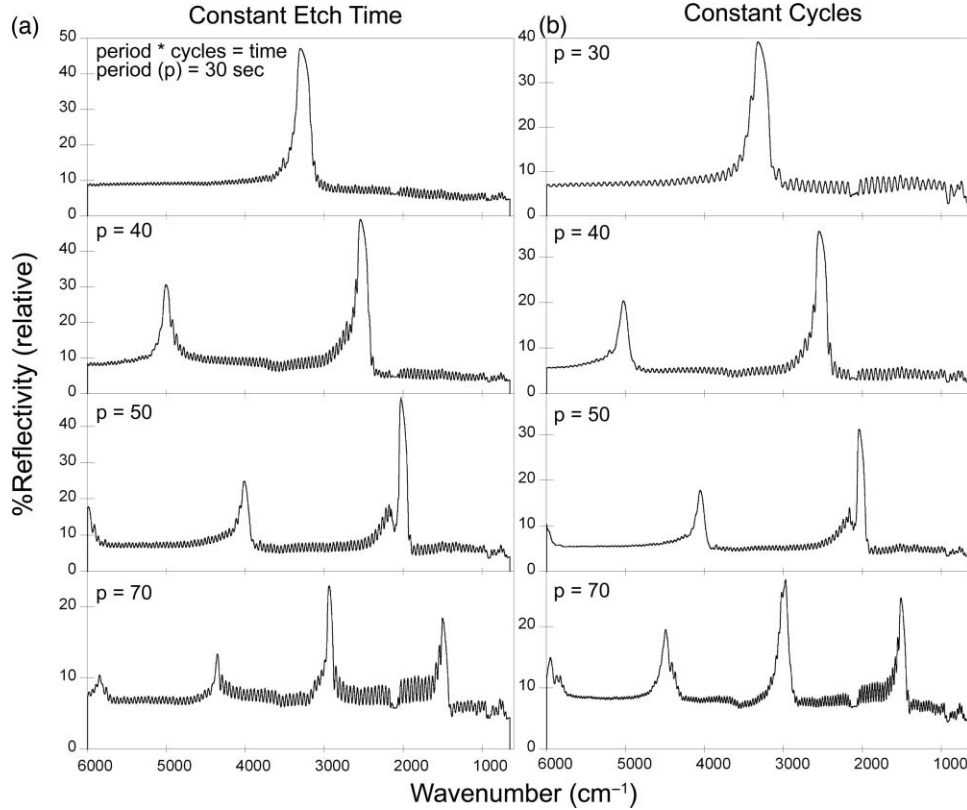
where  $\theta_a$  is the angle of propagation through the rugate filter and  $n_{\text{avg}} = 1.5$  is the average refractive index (calculated as described later). This yields an expected spectral position in reflectance mode at  $\theta_a = 12.5$  deg of  $1748 \text{ cm}^{-1}$ , with the observed difference due to the tolerance of the mirror positioning. The porous Si filter may be placed at any of the four beam diverter locations pictured in Fig. 1, but was placed after the gas sample cell for sensing experiments to simulate a filter on an infrared imaging device.

### 3.2 Effect of Rugate Repetitions

Increasing the number of sinusoid etch repetitions for a given fixed period reduces the height of the thin layer interference fringes relative to the rugate peak while increasing the etch thickness. Thicker layers result in increased absorption at porous Si-H absorption frequencies.

For the gas-sensing work above, layers with 45 rugate cycles were chosen as a nominal value exhibiting acceptable thin-film fringe reduction. Figure 3 displays spectra taken in reflectance mode of four etches with varying numbers of rugate cycles for a period of  $p = 43.7$  s. The effective optical thickness ( $2n_{\text{avg}}L$ ) increases linearly with the number of cycles due to the linear increase in the layer thickness  $L$ , for the constant average layer refractive index  $n_{\text{avg}}$ . This result indicates that issues affecting the etch rate of the porous layer do not dramatically deviate the linearity of the optical thickness with total etch time for very thick ( $> 50 \mu\text{m}$ ) etches.<sup>32</sup> Specifically, the diffusion of the HF electrolyte into the increasingly thicker film during long etches does not appear to have limited the etch rate.





**Fig. 4** Comparison of a series of etches with constant total etching times but with (a) a variable number of cycle repetitions to a series of etches with a constant number of sinusoid cycle repetitions but (b) with variable etching times. Spectra from structures of four of the sine-wave periods in each series are shown. The total etch time was equal to the period times (in seconds) the number of cycles. The two calibrations coincide at  $p = 50$  s, where each consisted of 45 repetitions and a total etch time of 2250 s.

### 3.3 Effect of the Etching Period

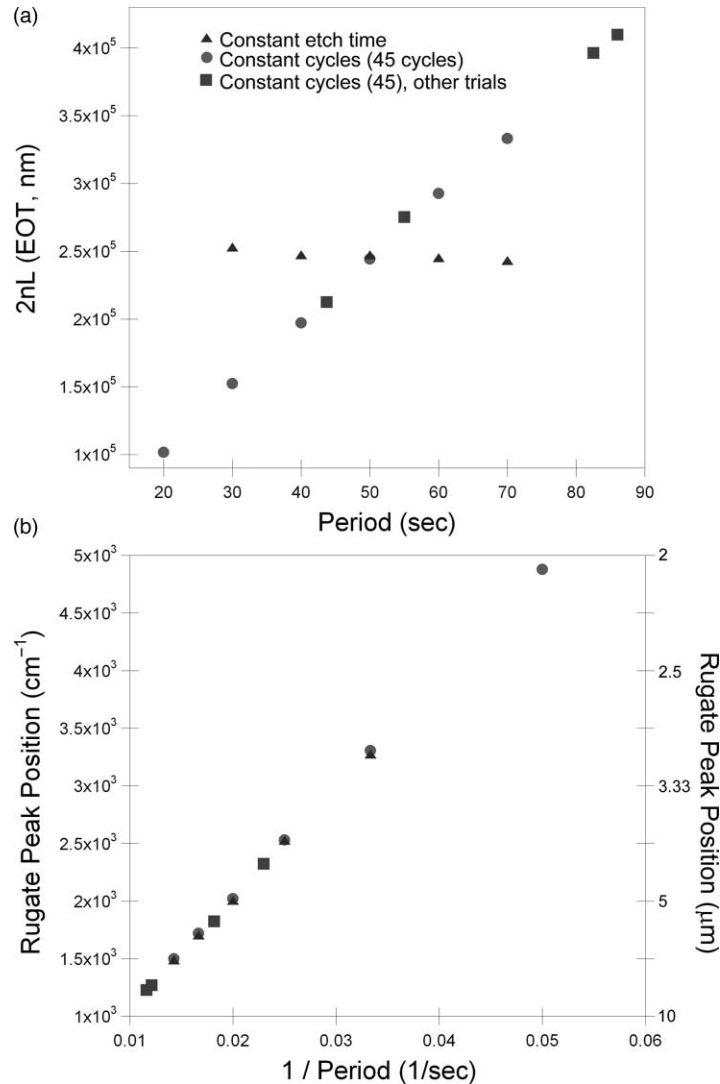
The period of the current-time etch wave, given in Eq. (2), corresponds directly to the spectral position of the rugate band, and rugates with spectral bands across the MWIR have been created. Figure 4 displays reflectance FTIR spectra of several of these filters.

The periodic variation of the current density with time given in Eq. (2) results in a periodic variation of the refractive index with depth  $z$ , expressed as<sup>3,4</sup>

$$n(z) = n_{\text{avg}} + \frac{\Delta n_{\text{avg}}}{2} \sin\left(\frac{4\pi n_{\text{avg}} z}{\lambda_0}\right) = n_{\text{avg}} + \frac{\Delta n}{2} \sin\left(\frac{2\pi z}{d}\right), \quad (5)$$

where  $n_{\text{avg}}$  is the average refractive index of the filter,  $n_{\text{avg}} z$  is the optical path,  $\lambda_0$  is the resonance peak wavelength of the rugate, and  $d$  is the spatial period of the index modulation; note that  $d$  is the physical thickness of one period. The spectral position of the rugate peak is expressed as  $\lambda_0 = 2n_{\text{avg}}d$ ; thus, longer periods in the current-time etching wave correspond to larger spatial periods and higher rugate peak wavelengths. As seen by comparing Eqs. (2) and (5), the location of the stop band  $\lambda_0$  is proportional to the period of the etching sine wave  $p$ , and thus, the frequency  $1/p$  scales with wavenumber ( $1/\lambda$ ). The refractive index profile with depth deviates somewhat from the sine waveform of the current etchwave because the etch rate increases with current, biasing the refractive index depth profile.<sup>33</sup> However, this bias is expected to be constant if the amplitude of the current-time wave is held constant and only the period is changed.





**Fig. 5** (a) Effective optical thickness versus the etchwave period for porous Si optical filters. Filters fabricated with a constant total etching time ( $\pi$ ) are compared to those etched for a constant number of sinusoid cycles ( $\bullet$  and  $\blacksquare$ ). (b) Position of the principal rugate spectral peak as a function of the frequency ( $1/\text{period}$ ) for both constant-time and constant-cycle repetition calibrations.

Figure 4 compares two sets of period versus peak wavelength ( $\lambda_0$ ) calibrations of MWIR porous Si filters, one in which the total etch time was held constant and the number of cycles varied [Fig. 4(a)], and the other in which the number of sinusoid cycles was held constant and the total etch time varied [Fig. 4(b)]. The two calibration series share a coincident point at a sine period of  $p = 50$  s. As expected, the etches with a constant total etch time have a similar spacing between the thin-film interference fringes, while the increasing thickness, and therefore optical thickness, of the constant-cycle etches results in a corresponding decrease in fringe spacing.

Figure 5 displays the effective optical thickness (EOT,  $2n_{\text{avg}}L$ ) and rugate peak position of these etches versus the period. The EOT was determined by an FFT of the thin-layer interference fringes in the visible spectrum. EOT values based on FFT of fringes in the infrared were also calculated and differed by a constant  $-4\%$  from the visible values obtained at normal

incidence. The filters with a constant total etch time display a slight decrease in effective optical thickness with the increasing period, in contrast to the linearly increasing EOT with period for constant-cycle, variable-etch-time filters, shown in Fig. 5(a). The EOT scales linearly with the period since for a constant  $n_{\text{avg}}$  of the layer, the thickness  $L$  is a direct function of the etch rate (in nanometers/second) multiplied by the etch time (in seconds). The rugate peak position of both the constant-time and constant-repeat etches is linear with etch period, as shown in Fig. 5(b). This is expected because  $\lambda_0$  scales with the period  $p$ , and thus, the quantity  $1/\lambda_0$  should scale with the frequency,  $1/p$ . Additional etches that were performed separately from the two trials above are included in Fig. 5 and show excellent agreement with these trends.

Several issues can affect the etch rate for longer etches and, consequently, the value of EOT and the spectral peak positions. HF diffusion to the etching boundary for thick layers can lead to a decrease in the layer growth rate with depth, and a reduction of the concentration of HF as it is consumed can influence the etch rate of long-duration etches with low electrolyte volumes.<sup>1,32</sup> To address this, the volume of HF was mixed and partially replaced every 5 min during an etching procedure. Incorporation of etch stops for 1 s every cycle to allow equilibration of electrolyte concentration showed no difference in optical properties or layer thickness, though others have utilized shorter etch stops to homogenize electrolyte distribution when creating  $\sim 300\text{-}\mu\text{m}$ -thick rugate filters with stop bands at terahertz frequencies.<sup>19</sup> Furthermore, after a section of the filter has been electrochemically etched, it will continue to dissolve at a much lower rate while in contact with HF, leading to a high- to low-porosity gradient from the top to bottom of the etched layer. The linearity of the EOT and peak position in Fig. 5 with increasingly thicker etches and longer etch times (increasing periods for constant cycles) indicate that these issues were not significant for the samples under investigation here. The gravimetric porosity was determined for all etched layers as 74%, with no more than a  $\pm 1\%$  variation across all samples, attributable to error in the weighing of the samples. The porosity exhibited no trend with changes in period, indicating uniformity of the etch rate with increasing etch time of the samples. It is also worth noting the decrease in the width of the rugate peaks in the FTIR spectra with increasing period. This is an expected result of changing the reflectance band position because the width of the spectral band  $\Delta\lambda$  centered at  $\lambda_0$  can be expressed as<sup>12,34</sup>

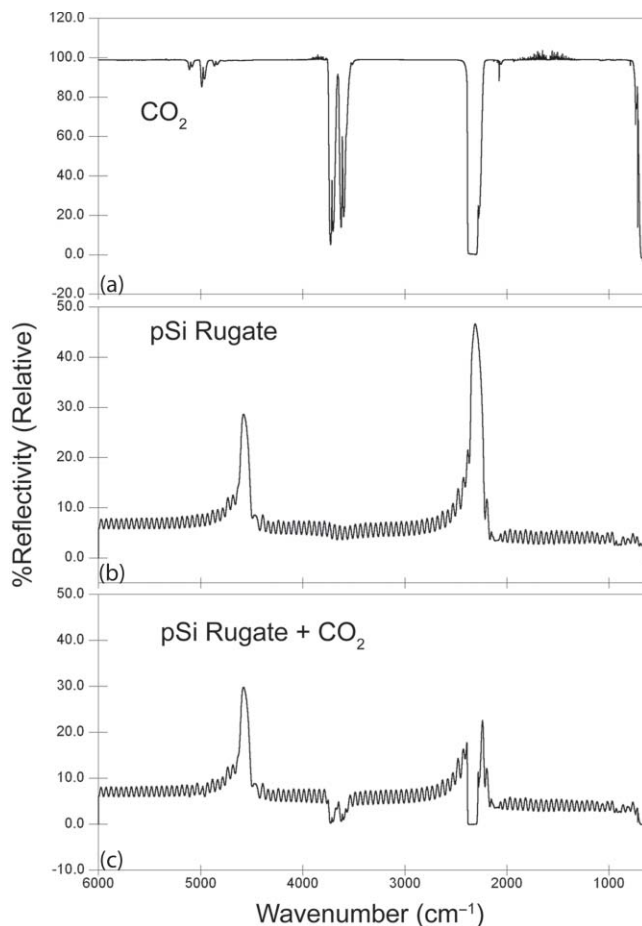
$$\frac{\Delta\lambda}{\lambda_0} = \frac{\Delta n}{2n_{\text{avg}}}. \quad (6)$$

Because the variation in refractive index  $\Delta n$  and average refractive index of the layer  $n_{\text{avg}}$  are determined by the low and high etch currents of the sine etching wave and do not change with period, an increase in the wavenumber  $1/\lambda_0$  of the stop band results in a commensurate decrease of the rugate peak  $1/\Delta\lambda$ , as seen in the FTIR spectra of Fig. 4.

The SEM thickness and effective optical thickness ( $2n_{\text{avg}}L$ ) of a filter specimen can be used to determine the average refractive index  $n_{\text{avg}}$  of the porous filter. For the single-peak  $\text{CO}_2$  sensor example with a thickness of  $70.7\ \mu\text{m}$ ,  $n_{\text{avg}} = 1.51$ . The refractive index of the silicon pillars in the porous material,  $n_{\text{Si}}$ , was then determined as 3.67 using the two-component Bruggeman effective medium approximation,<sup>33</sup> using a value of EOT determined from the optical interference spectrum between 850 and 1000 nm. This is a close match to the literature value of  $n = 3.6$  at 900 nm.<sup>35</sup> This agreement indicates that the optical properties of the filters tuned to MWIR wavelengths are consistent with expected porous silicon properties.

### 3.4 Demonstration of Gas Sensing with a Single-Peak Rugate

A rugate filter tuned to the  $\nu(\text{CO}_2)$  band is shown in Fig. 6. The  $\text{CO}_2$  vibrational bands between 2260 and 2390  $\text{cm}^{-1}$  are easily observed in a reference sample of the gas taken without the porous Si filter by using silver mirrors at all beam deflection locations. The slight sawtoothing



**Fig. 6** Reflectance-mode FTIR spectra demonstrating a porous Si rugate filter containing an in-band and an out-of-band peak for detection of  $\text{CO}_2$ . The rugate was etched with a single-frequency sinusoidal current-time waveform with a period  $p = 43.7$  s. (a) Gas chamber purged with  $\text{CO}_2$ , with silver mirrors mounted in all four beam deflection locations (see Fig. 1). (b) Gas cell purged with  $\text{N}_2$ , with porous Si filter mounted at the deflection position indicated in Fig. 1. The sample was prepared such that one of the stop-band resonances appears at  $\sim 2300$   $\text{cm}^{-1}$ , coinciding with the C–O stretching band of  $\text{CO}_2$ . The other peak (at  $\sim 4600$   $\text{cm}^{-1}$ ) is an overtone band. (c) Gas cell purged with  $\text{CO}_2$ , with porous Si at the beam deflection position indicated in Fig. 1.

visible around  $2350$   $\text{cm}^{-1}$  is due to incompletely resolved Q and R absorption branches (FTIR resolution was  $2$   $\text{cm}^{-1}$ ). The absorptions at higher wavenumbers are the result of combination vibrational modes, with a doublet at  $2.7$   $\mu\text{m}$  and higher members of the same sequence at  $2.0$   $\mu\text{m}$ .<sup>6,7</sup> The signals observed from  $1400$  to  $1800$   $\text{cm}^{-1}$  is due to a small amount of residual water vapor in the FTIR chamber.

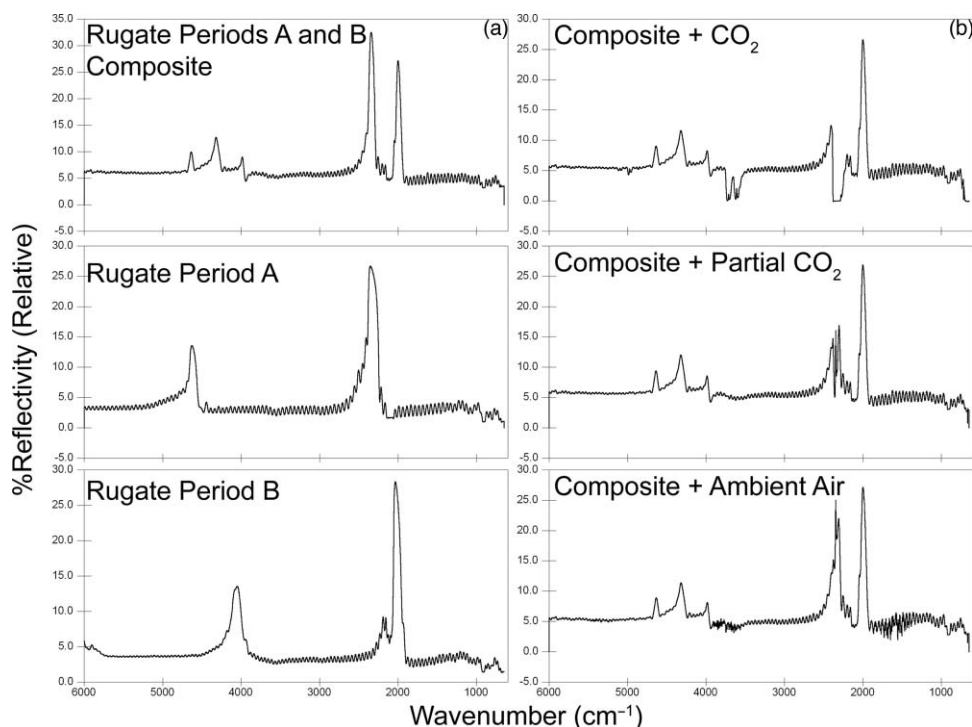
The rugate filter displayed in Fig. 6 was constructed with a current-time sinusoid waveform with a period of  $43.7$  s etched for 45 repetitions, designed to match the  $2350$   $\text{cm}^{-1}$  principal absorption band. The resulting filter exhibited a cross-sectional thickness of  $70.7$   $\mu\text{m}$ . On introduction of  $\text{CO}_2$  to the gas cell, the principal rugate band was obscured by the absorbing molecules, decreasing the peak area, while the higher order harmonic was unchanged. The ratio of the areas or of the intensities of the principal peak to the harmonic overtone peak can thus be used as a referenced sensor for the presence of  $\text{CO}_2$ .

### 3.5 Gas Sensing with a Composite Rugate

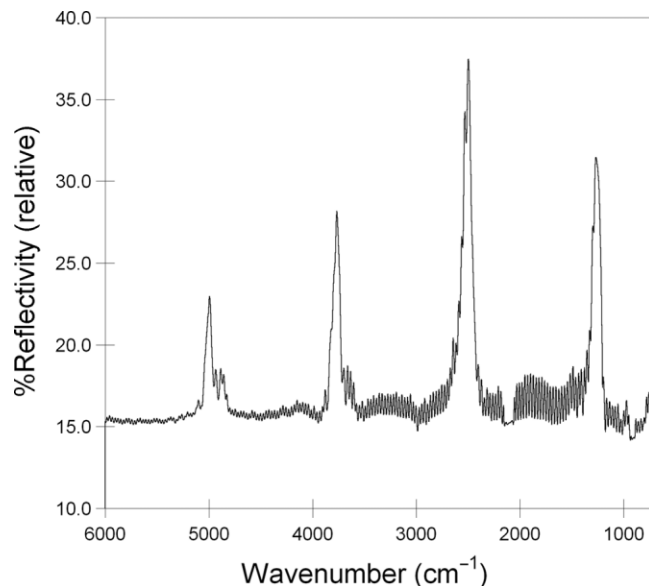
In the single-peak rugate described earlier, a harmonic band was utilized as a reference channel for the principal rugate band at  $2350\text{ cm}^{-1}$  that overlaps the  $\text{CO}_2$  absorptions. The location of the harmonic band is spectrally distant from the principal peak and its location depends on the principal peak location. To introduce a tunable reference peak that is spectrally closer to the principal band, a composite, infrared rugate was fabricated consisting of a single layer combining two sinusoidal current-time frequencies into the current-time etch wave, as pictured in Fig. 7. Filters of each single frequency were fabricated for reference [Fig. 7(a)], with the composite filter comprised of  $p = 43.7\text{ s}$  and  $p = 51\text{ s}$  periods that resulted in rugate bands at  $2350$  and  $2000\text{ cm}^{-1}$  respectively, with a total layer thickness of  $72.5\text{ }\mu\text{m}$  determined by SEM. As shown in Fig. 7(b), the presence of  $\text{CO}_2$  in the gas cell greatly reduced the area of the peak at  $2350\text{ cm}^{-1}$ , while not affecting the reference channel at  $2000\text{ cm}^{-1}$ . Figure 7 also demonstrates sensing of  $\text{CO}_2$  at lower concentrations. A spectrum reflected off the filter was taken for a 50/50 volumetric mixture of  $\text{CO}_2$  and  $\text{N}_2$  in the gas cell, as well as ambient room air. The reflectance scan of the latter exhibits a slight reduction in the  $2350\text{ cm}^{-1}$  peak area and shows evidence of water vapor outside the rugate bands.

### 3.6 Matching P=O Bond Stretching Modes

To demonstrate the ability to tune rugate peaks to the edge of the long-wave infrared region, a filter was constructed to match a typical P=O stretching vibration at  $1250\text{ cm}^{-1}$ . This transition is present in the G-series chemical nerve agents sarin, soman, tabun, and VX.<sup>9,10</sup> The filter



**Fig. 7** Reflectance-mode FTIR detection of  $\text{CO}_2$  using a multi-frequency rugate optical filter. (a) Single-frequency components with  $p = 43.7\text{ s}$  (middle) and  $p = 51\text{ s}$  (bottom) compared to the composite filter (top). (b) Spectra of the composite filter with varying levels of  $\text{CO}_2$  in the gas sample cell: fully purged with  $\text{CO}_2$  (top), 50%  $\text{CO}_2$ /50%  $\text{N}_2$  (middle), and an ambient level of  $\text{CO}_2$  from room air (bottom).



**Fig. 8** Reflectance-mode FTIR of an optical filter with a sine current-time etching waveform period of  $p = 82.5$  s mounted at one of the beam diversion positions. The principal rugate peak at  $1250\text{ cm}^{-1}$  was designed to match the P=O bond stretch of G-series chemical nerve agents.

shown in Fig. 8 was etched with a sinusoid current-time period of  $p = 82.5$  s, resulting in a  $123\text{-}\mu\text{m}$ -thick layer as determined by SEM. Several overtone bands are clearly present.

## 4 Conclusions

Optical rugate filters with reflectance bands in the medium-wave infrared were successfully fabricated from porous silicon and used to detect  $\text{CO}_2$ , by matching the reflectance peak to a vibrational absorbance band of the molecule. Filters with rugate bands tuned across the MWIR region were fabricated, including porous layers with an optical band at the wavelength of a typical P=O bond stretch at  $1250\text{ cm}^{-1}$ , and the spectral position of the sensing layer reflectivity band in the infrared exhibited excellent linearity with the frequency of the current-time sinusoid etching waveform.

## Acknowledgments

This material is based on work supported by the National Science Foundation under Grant No. DMR-0806859.

## References

1. L. Canham, *Properties of Porous Silicon*, Vol. 18, pp. 1–405, Short Run Press Ltd., London (1997).
2. A. Janshoff, K. P. S. Dancil, C. Steinem, D. P. Greiner, V. S. Y. Lin, C. Gurtner, K. Motesharei, M. J. Sailor, and M. R. Ghadiri, “Macroporous p-type silicon Fabry-Perot layers. Fabrication, characterization, and applications in biosensing,” *J. Am. Chem. Soc.* **120**, 12108–12116 (1998).
3. E. Lorenzo, C. J. Oton, N. E. Capuj, M. Ghulinyan, D. Navarro-Urrios, Z. Gaburro, and L. Pavesi, “Porous silicon-based rugate filters,” *Appl. Opt.* **44**, 5415–5421 (2005).
4. W. E. Johnson and R. L. Crane, “Introduction to rugate filter technology,” *Proc. SPIE* **2046**, 88–108 (1993).

5. S. O. Meade, M. S. Yoon, K. H. Ahn, and M. J. Sailor, "Porous silicon photonic crystals as encoded microcarriers," *Adv. Mater.* **16**, 1811–1814 (2004).
6. P. E. Martin and E. F. Barker, "The infrared absorption spectrum of carbon dioxide," *Phys. Rev.* **41**, 291–303 (1932).
7. R. C. Herman, "Vibrational energy levels of the carbon dioxide molecule," *Astrophys. J.* **107**, 386–388 (1948).
8. V. Zeninari, A. Vicet, B. Parvitte, L. Joly, and G. Durry, "In situ sensing of atmospheric CO<sub>2</sub> with laser diodes near 2.05  $\mu$  m: A spectroscopic study," *Infr. Phys. Tech.* **45**, 229–237 (2004).
9. M. T. Soderstrom and R. A. Ketola, "Identification of nerve agents and their homologs and dialkyl methylphosphonates by gas-chromatography-Fourier-transform infrared spectrometry (GC-FTIR). 1. spectral interpretation," *Fres. J. Anal. Chem.* **350**, 162–167 (1994).
10. E. H. Braue and M. G. Pannella, "FT-IR analysis of chemical warfare agents," *Mikrochim. Acta* **1**, 11–16 (1988).
11. M. Deubel, G. Von Freymann, M. Wegener, S. Pereira, K. Busch, and C. M. Soukoulis, "Direct laser writing of three-dimensional photonic-crystal templates for telecommunications," *Nat. Mater.* **3**, 444–447 (2004).
12. A. G. Imenes and D. R. McKenzie, "Flat-topped broadband rugate filters," *Appl. Opt.* **45**, 7841–7850 (2006).
13. J. Chapron, S. A. Alekseev, V. Lysenko, V. N. Zaitsev, and D. Barbier, "Analysis of interaction between chemical agents and porous Si nanostructures using optical sensing properties of infra-red Rugate filters," *Sens. Actuat. B* **120**, 706–711 (2007).
14. P. L. Swart, P. V. Bulkin, and B. M. Lacquet, "Rugate filter manufacturing by electron cyclotron resonance plasma-enhanced chemical vapor deposition of SiN<sub>x</sub>," *Opt. Eng.* **36**, 1214–1219 (1997).
15. K. Robbie, A. J. P. Hnatiw, M. J. Brett, R. I. MacDonald, and J. N. McMullin, "Inhomogeneous thin film optical filters fabricated using glancing angle deposition," *Electron. Lett.* **33**, 1213–1214 (1997).
16. W. J. Gunning, R. L. Hall, F. J. Woodberry, W. H. Southwell, and N. S. Gluck, "Codeposition of continuous composition rugate filters," *Appl. Opt.* **28**, 2945–2948 (1989).
17. K. Kaminska, T. Brown, G. Beydaghyan, and K. Robbie, "Vacuum evaporated porous silicon photonic interference filters," *Appl. Opt.* **42**, 4212–4219 (2003).
18. N. Ishikura, M. Fujii, K. Nishida, S. Hayashi, and J. Diener, "Porous silicon based extended-bandwidth rugate filters for mid-infrared application," *Infr. Phys. Tech.* **53**, 292–294 (2010).
19. S. Z. A. Lo and T. E. Murphy, "Nanoporous silicon multilayers for terahertz filtering," *Opt. Lett.* **34**, 2921–2923 (2009).
20. G. Sando and J. Dubois, "Seeing" the chemicals in pharmaceutical tablets with NIR chemical imaging," *Chim. Oggi-Chem. Today* **28**, 40–42 (2010).
21. A. F. H. Goetz and B. Curtiss, "Hyperspectral imaging of the Earth: Remote analytical chemistry in an uncontrolled environment," *Field Anal. Chem. Tech.* **1**, 67–76 (1996).
22. A. I. Dsouza, L. C. Dawson, E. J. Anderson, A. D. Markum, W. E. Tennant, L. O. Bubulac, M. Zandian, J. G. Pasko, W. V. McLevige, D. D. Edwall, J. W. Derr, and J. E. Jandik, "VSWIR to VLWIR MBE grown HgCdTe material and detectors for remote sensing applications," *J. Electron. Mater.* **26**, 656–661 (1997).
23. A. Rogalski, J. Antoszewski, and L. Faraone, "Third-generation infrared photodetector arrays," *J. Appl. Phys.* **105**, 091101 (2009).
24. A. D. Stiff-Roberts, "Quantum-dot infrared photodetectors: a review," *J. Nanophoton.* **3**, 031607 (2009).
25. S. D. Gunapala, S. V. Bandara, J. K. Liu, J. M. Mumolo, D. Z. Ting, C. J. Hill, J. Nguyen, B. Simolon, J. Woolaway, S. C. Wang, W. P. Li, P. D. LeVan, and M. Z. Tidrow,



- “Demonstration of megapixel dual-band QWIP focal plane array,” *IEEE J. Quant. Electron.* **46**, 285–293 (2009).
26. J. M. Xu, “Highly ordered carbon nanotube arrays and IR detection,” *Infr. Phys. Tech.* **42**, 485–491 (2001).
  27. S. Ilyas, T. Bocking, K. Kilian, P. J. Reece, J. Gooding, K. Gaus, and M. Gal, “Porous silicon based narrow line-width rugate filters,” *Opt. Mater.* **29**, 619–622 (2007).
  28. L. M. Shao, C. W. Roske, and P. R. Griffiths, “Detection of chemical agents in the atmosphere by open-path FT-IR spectroscopy under conditions of background interference: I. High-frequency flashes,” *Anal. Bioanal. Chem.* **397**, 1511–1519 (2010).
  29. M. Tahtouh, J. R. Kalman, C. Roux, C. I. Lennard, and B. J. Reedy, “The detection and enhancement of latent fingerprints using infrared chemical imaging,” *J. Forens. Sci.* **50**, 64–72 (2005).
  30. A. Halimaoui, “Porous silicon formation by anodisation,” in *Properties of Porous Silicon*, Vol. 18, pp. 12–22, L. Canham, Ed., Short Run Press Ltd., London (1997).
  31. C. Pacholski, M. Sartor, M. J. Sailor, F. Cunin, and G. M. Miskelly, “Biosensing using porous silicon double-layer interferometers: Reflective interferometric Fourier transform spectroscopy,” *J. Am. Chem. Soc.* **127**, 11636–11645 (2005).
  32. V. Lehmann, *Electrochemistry of Silicon*, pp. 51–75, Wiley-VCH, Weinheim, Germany (2002).
  33. M. S. Salem, M. J. Sailor, T. Sakka, and Y. H. Ogata, “Electrochemical preparation of a rugate filter in silicon and its deviation from the ideal structure,” *J. Appl. Phys.* **101**, 063503 (2007).
  34. H. A. Abusafia, A. I. Alsharif, and I. O. Abualjarayesh, “Rugate filter sidelobe suppression using half-apodization,” *Appl. Opt.* **32**, 4831–4835 (1993).
  35. E. D. Palik, *Handbook of Optical Constants of Solids*, p. 337, Academic Press, New York (1998).

Biographies and photographs of the authors not available.